

# CORAL: Solving Complex Constraints for Symbolic PathFinder

Matheus Souza,

Mateus Borges,

Marcelo d'Amorim\*

Corina Pasareanu

Federal University of Pernambuco  
Recife-PE, Brazil

CMU SV/NASA Ames Research Center  
Moffet Field-CA, USA

\* presenter

# Context and Problem

- Context
  - Symbolic execution (SE)
- Problem

Program analysis technique to generate test input data for achieving high path coverage.

```
foo(int x) {  
    x = x + 1;  
    if (x > 10) {  
        // ...  
    } else {  
        // ...  
    }  
}
```

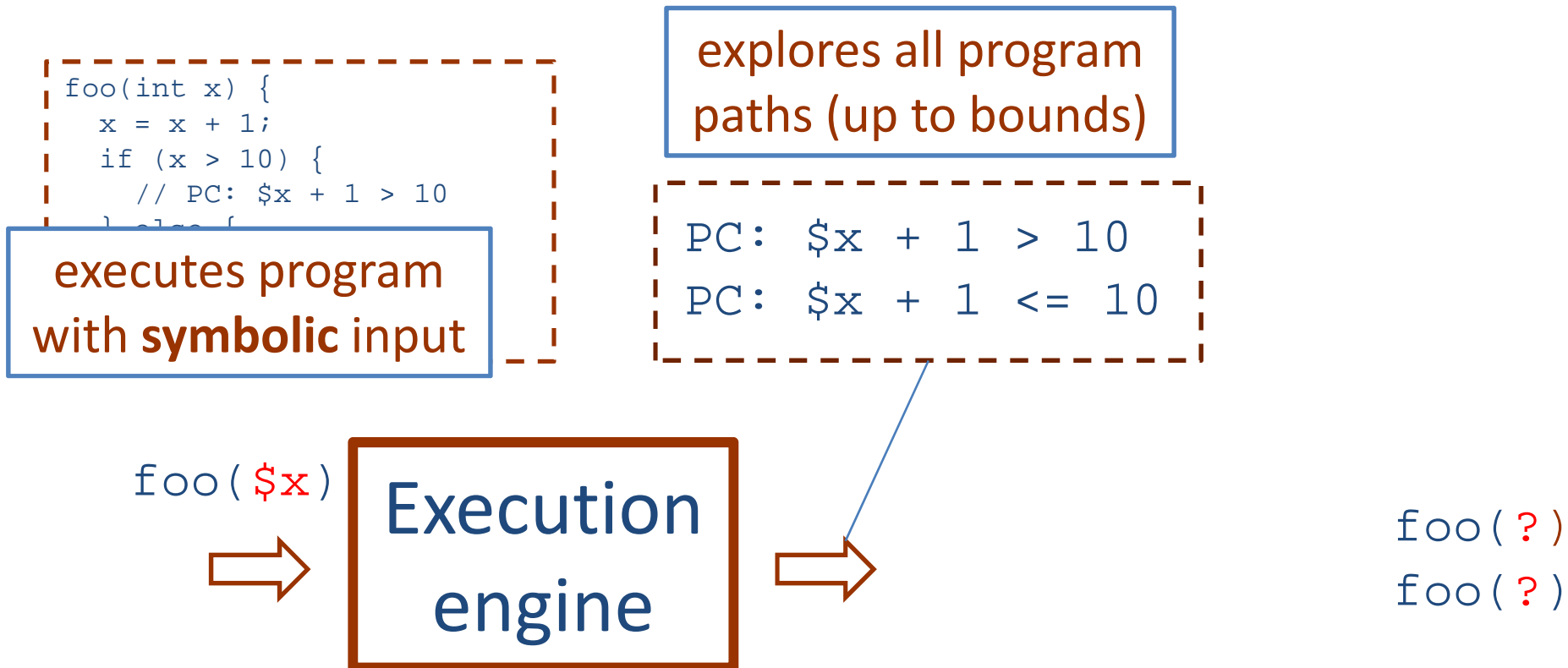
foo(?)

foo(?)

# Context and Problem

- Context
  - Symbolic execution (SE)
- Problem

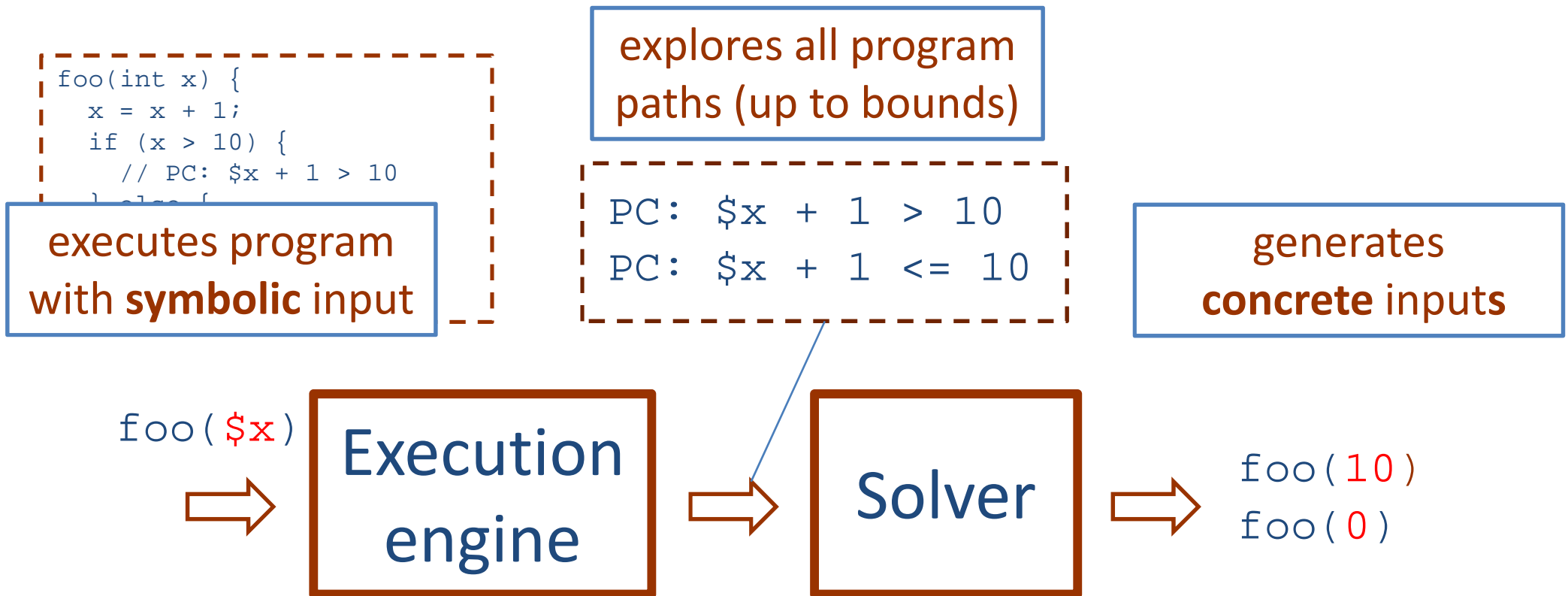
Program analysis technique to generate test input data for achieving high path coverage.



# Context and Problem

- Context
  - Symbolic execution (SE)
- Problem

Program analysis technique to generate test input data for achieving high path coverage.



# Context and Problem

- Context
  - Symbolic execution (SE)
- Problem
  - Inability of solvers to deal with complex constraints

```
foo(double x) {  
  x = x + 1;  
  if (x > Math.pow(Math.sin(x),2)){  
    // PC: $x + 1 > ($x + 1)^2  
  } else {  
    // PC: $x + 1 <= ($x + 1)^2  
  }  
}
```

undecidable or computationally  
complex solving

```
PC: $x + 1 > sin($x + 1)^2  
PC: $x + 1 <= sin($x + 1)^2
```

foo(\$x)



Execution  
engine



Solver



foo(?)  
foo(?)

# Context and Problem

- **Context**
  - Symbolic execution (SE)
- Problem
  - Inability of solvers to deal with

Program analysis technique to generate test input data for achieving high path coverage.

**Implemented in Symbolic PathFinder (SPF) and used at NASA and Fujitsu.**

# Note about SPF

- Model-level interpretation of calls to math functions

$$\$x + 1 \longrightarrow \mathit{sin} \longrightarrow \mathit{sin}(\$x + 1)$$

Symbolic expression denoting  
the result value of the call

# CORAL solvers

- **Target applications:** SE of programs that manipulate floating-point variables
  - Use floating-point arithmetic
  - Call specific math functions (from `java.lang.Math`)

Common in software from NASA.

$\text{sqrt}(\text{exp}(x+z)) < \text{pow}(z, x),$   
 $x > 0, y > 1, z > 1, y < x+2,$   
 $w = x+2$



$\{x=4.31, y=6.08,$   
 $z=9.51, w=6.31\}$

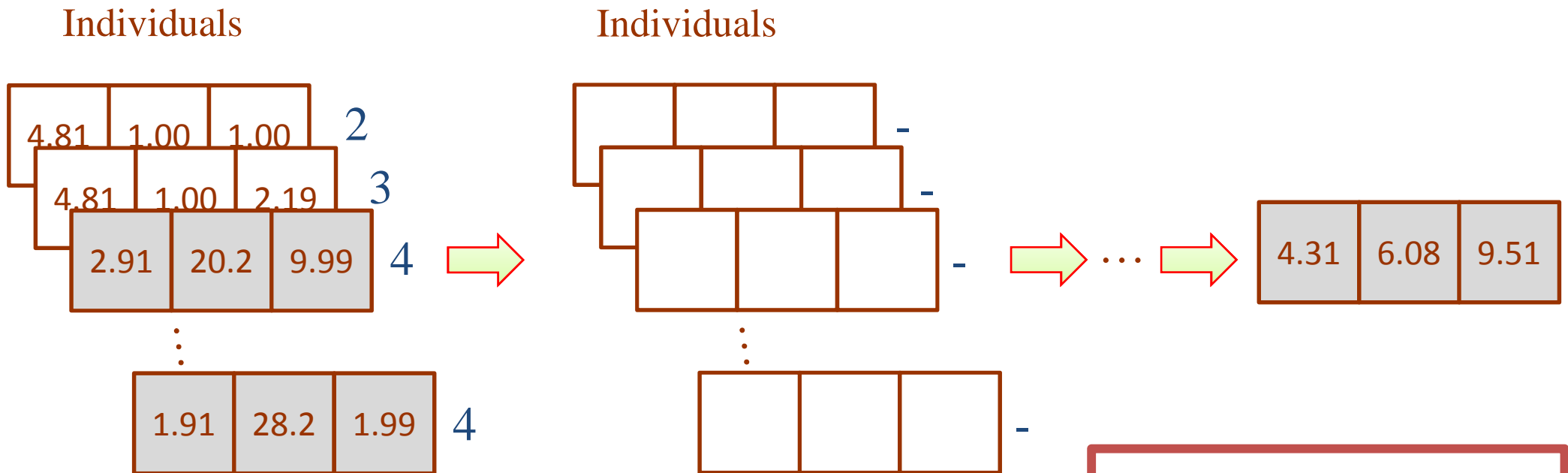


# Summary about CORAL

- Meta-heuristic solver
  - Distance-based fitness function
- Optimizations
  - Identification of dependent variables
  - Inference of variable domains
  - Efficient evaluation of constraints

# Quick outlook on heuristic search

**Input:**  $\text{sqrt}(\text{exp}(x+z)) < \text{pow}(z, x)$  ,  $x > 0$ ,  $y > 1$ ,  $z > 1$ ,  $y < x+2$   
**Solution:** ?



Identify best fit individuals

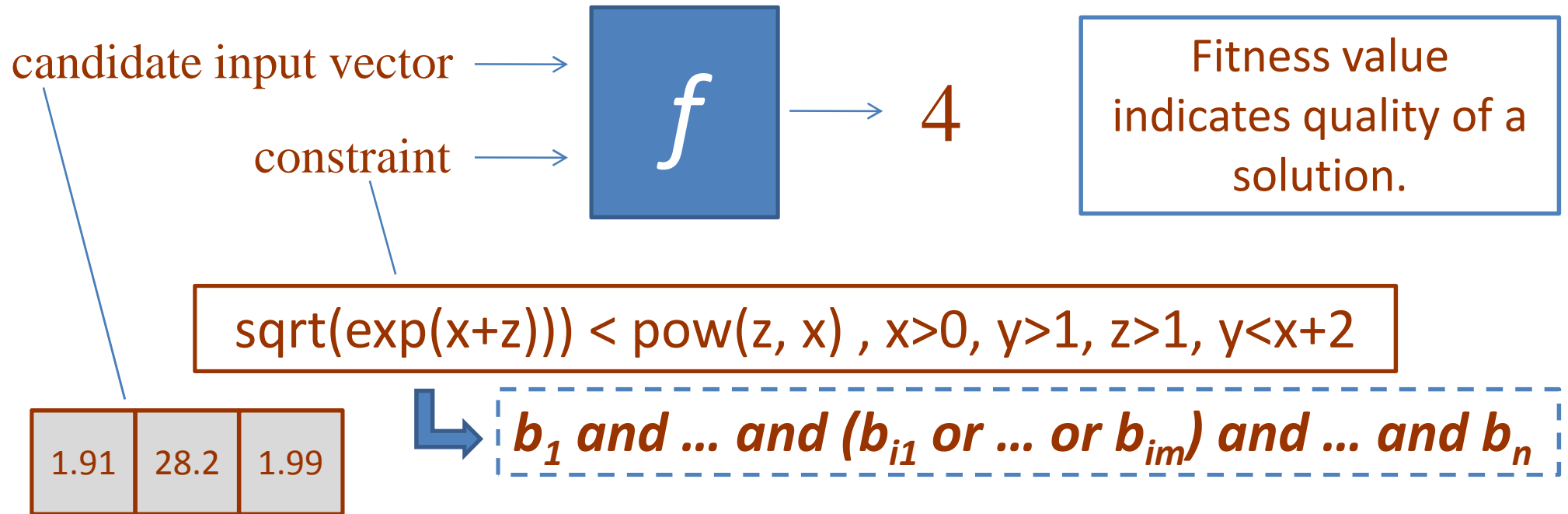
create new generations

stop after num. iterations or solution found

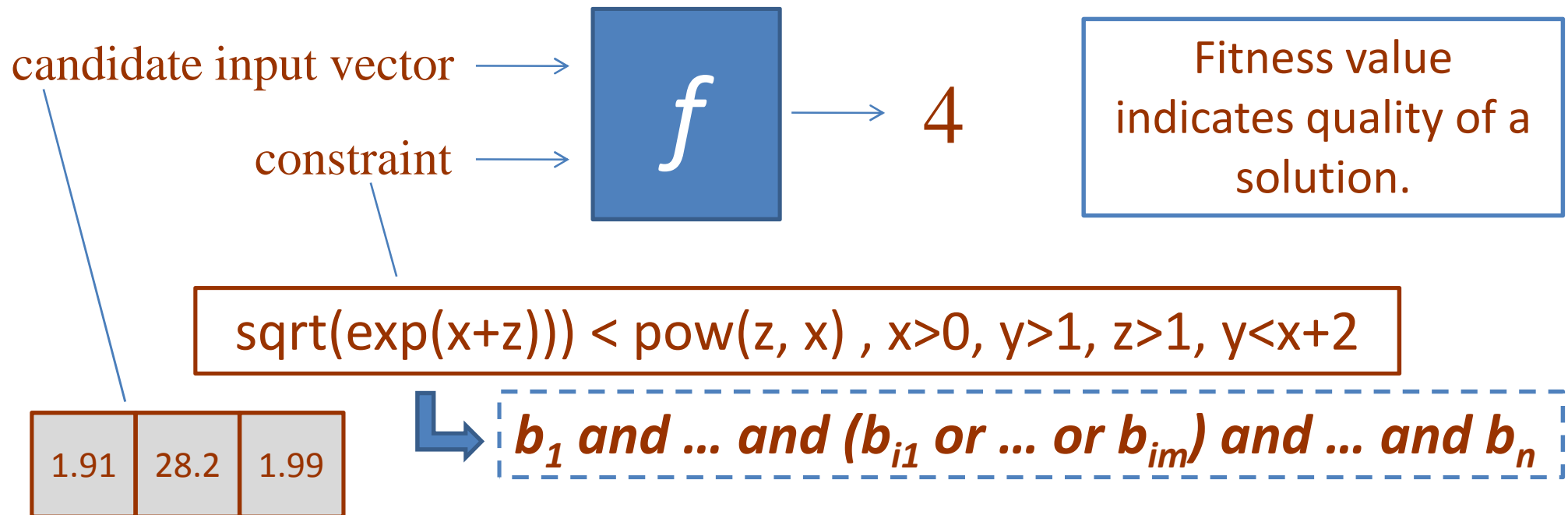
# Particle swarm optimization (PSO)

- Similar to GA, but with fixed-sized population
  - Search simulates movements in a group of animals
    - Implemented very efficiently (matrix operations)
    - Parameters to calibrate local and global influence
- Used opt4j library (see [opt4j.sourceforge.net](http://opt4j.sourceforge.net))

# Fitness Function



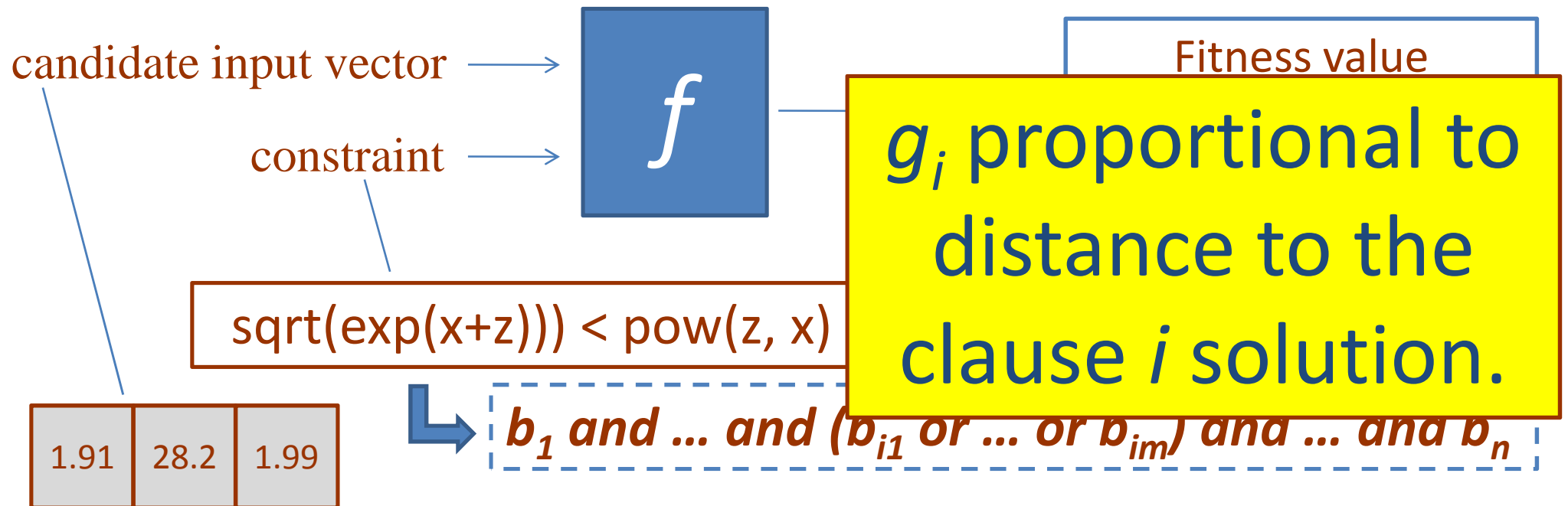
# Fitness Function



$$f(\vec{x}) = \sum_i w_i * g_i(\vec{x})$$

$$g_i(\vec{x}) = \max_{1 < j < m} 1 - d(b_{ij}, \vec{x})$$

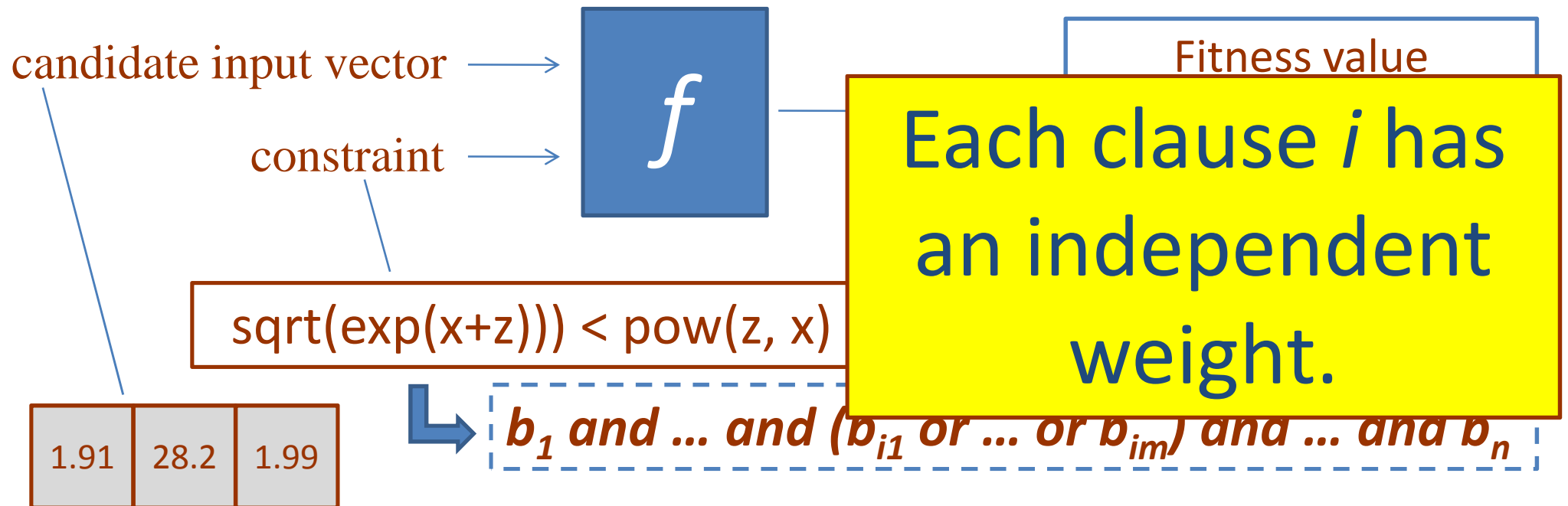
# Fitness Function



$$f(\vec{x}) = \sum_i w_i * g_i(\vec{x})$$

$$g_i(\vec{x}) = \max_{1 < j < m} 1 - d(b_{ij}, \vec{x})$$

# Fitness Function



$$f(\vec{x}) = \sum_i w_i * g_i(\vec{x})$$

$$g_i(\vec{x}) = \max_{1 < j < m} 1 - d(b_{ij}, \vec{x})$$

# RESULTS



# Evaluation

- Impact of search algorithm and optimization
- Effectiveness to solve...
  - simple constraints
  - complex constraints
- NASA case studies
  - PISCES
  - Apollo Lunar Autopilot

# Impact of search and optimizations

- Comparison of 4 variations of CORAL
  - {PSO,Random} x {optimized, non-optimized}

	pso-opt	pso	random-opt	random
pso-opt	-	74	88	257
pso	13	-	71	196
random-opt	3	47	-	180
random	0	0	8	-

Number of constraints that solver on row 4 solved and solver on column 3 did not solve

# Impact of search and optimizations

- Comparison of 4 variations of CORAL
  - {PSO,Random} x {optimized, non-optimized}

	pso-opt	pso	random-opt	random
pso-opt	-	<b>74</b>	88	257
pso	<b>13</b>	-	71	196
random-opt	3	47	-	<b>180</b>
random	0	0	<b>8</b>	-

optimization pays off on average

# Impact of search and optimizations

- Comparison of 4 variations of CORAL
  - {PSO,Random} x {optimized, non-optimized}

	pso-opt	pso	random-opt	random
pso-opt	-	74	88	257
pso	<b>13</b>	-	71	196
random-opt	<b>3</b>	47	-	180
random	<b>0</b>	0	8	-

pso-opt performs better on average

# Effectiveness on simple constraints

- Constraints involving decidable theories
  - Bounded-exhaustive testing of BST and Treemap
- Compared CORAL with Choco, CVC3, and Yices

CORAL could solve as many constraints as any other.

# Effectiveness on complex constraints

- 78 manually-written test cases with math functions
- Compared CORAL with Choco
- CORAL solved 92.3% of the constraints (707/766)

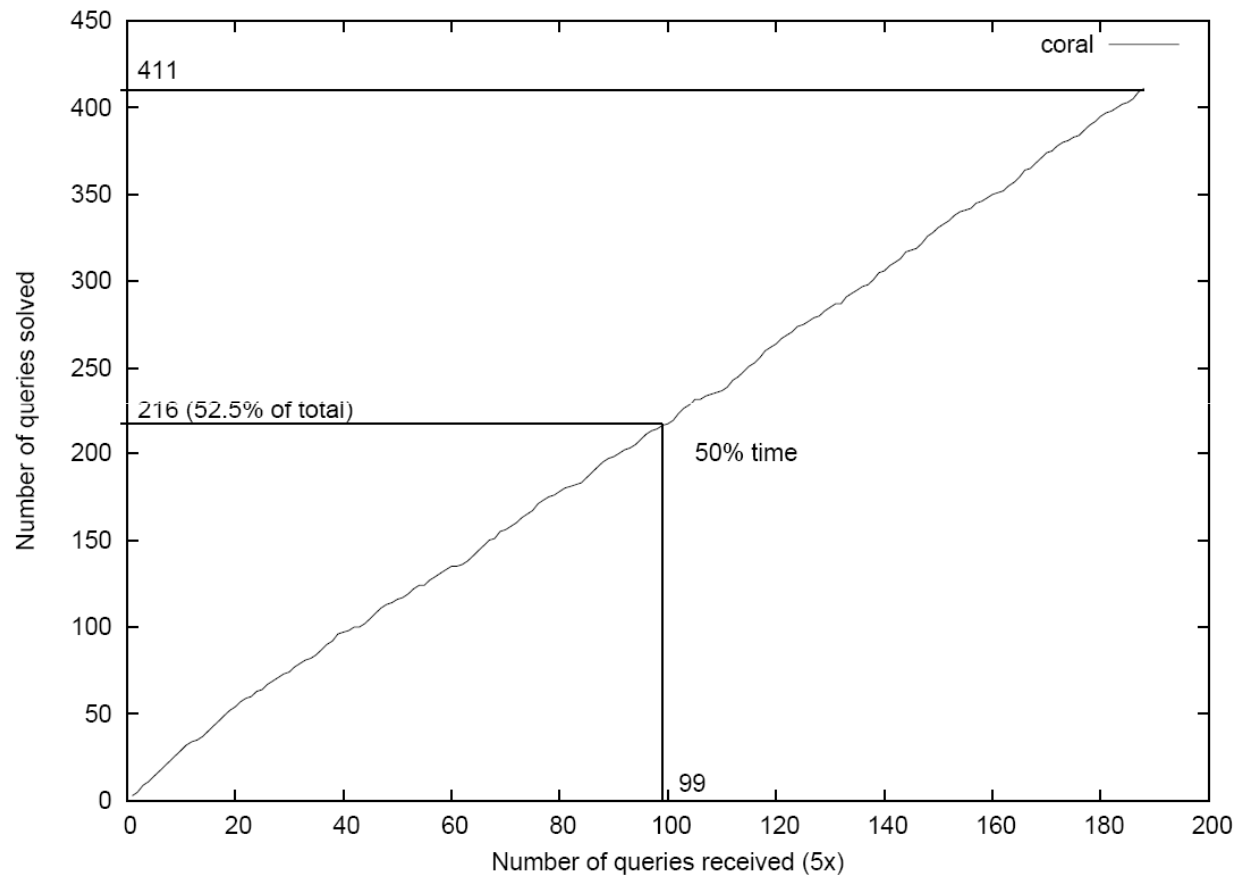
For no query CHOCO could solve and CORAL could not.

# PISCES

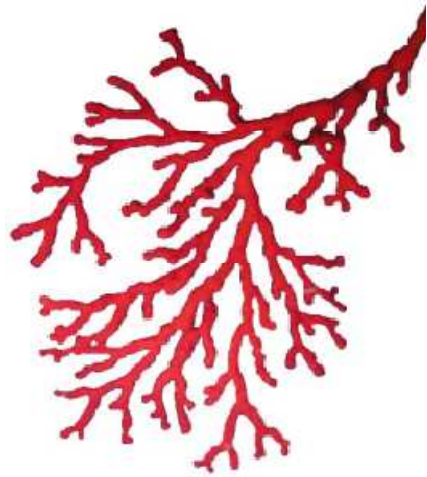
- PISCES library
  - Some of the computations involved: hyperbolic (arc) sine, cosine, tangent, floating point remainder.
- Analyzed 20 methods with SPF+CORAL
- Found undocumented pre-conditions
  - Illegal arguments not properly caught in code

# Apollo Lunar Autopilot

- Simulink model translated to Java
- Bounds
  - max. time = 2h, max. path condition length = 50







CORAL

**For more information visit**



[pan.cin.ufpe.br/coral](http://pan.cin.ufpe.br/coral)